

# **An Objective Model of Localisation in Binaural Sound Reproduction Systems**

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# Outline

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- HRIR based Binaural Sound Reproduction Systems using Ambisonic
- Definitions
- Mathematical Model
- Results
- Outlook

# Binaural Systems using Ambisonic

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## Binaural Reproduction Systems:

- filtering virtual source signals with HRIRs
- incorporate head tracking to improve source localisation

## Problem:

- time-varying interpolation between HRIRs

# Binaural Systems using Ambisonic

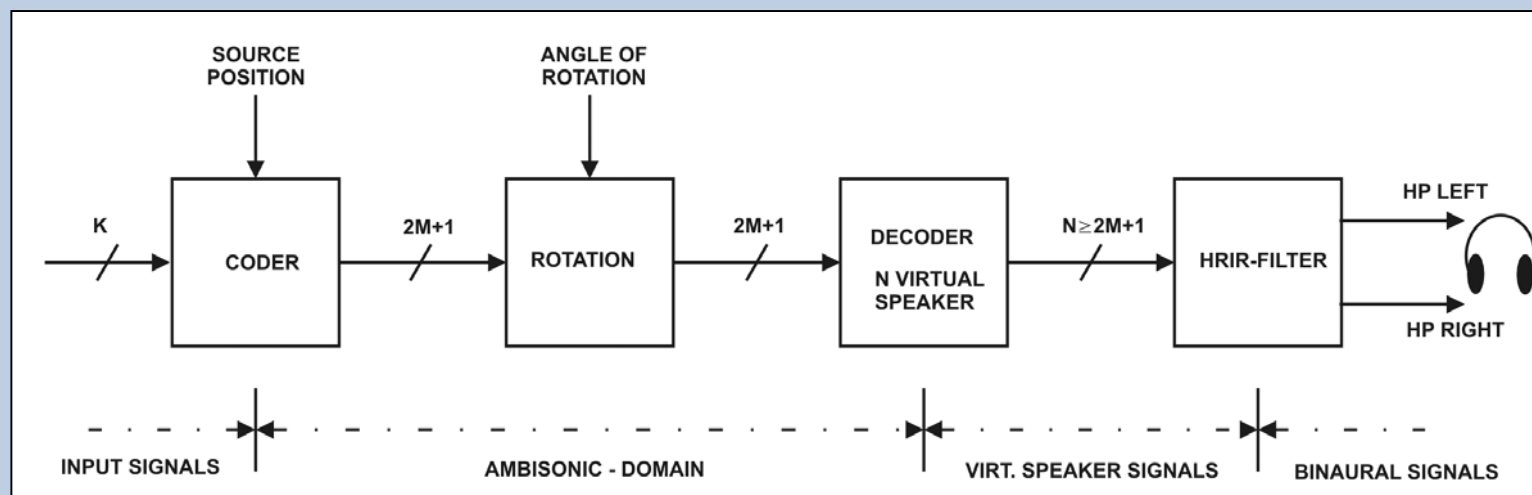
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## Why Ambisonic?

- head movement:
  - time-invariant HRIR filter
  - cheap time-variant rotation matrix
- decoding is independent from coding
- number of transmit channels is independent from number of virtual sources

# Binaural Systems using Ambisonic

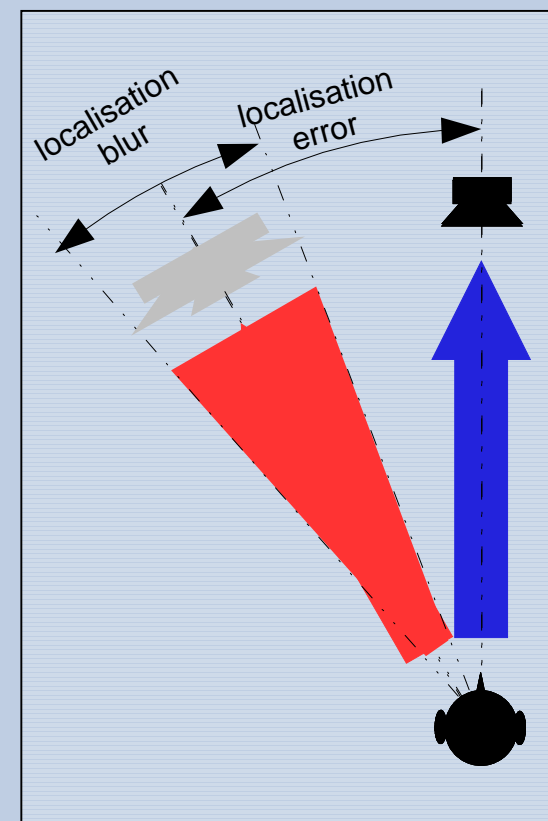
- encode signals depending on source position
- rotate Ambisonic depending on head position
- decode Ambisonic to virtual speaker signals
- convolve speaker signals with HRIRs



# Definitions

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- localisation function
- localisation error
- localisation blur
- average localisation error
- average localisation blur



# Mathematical Model

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## Intentions:

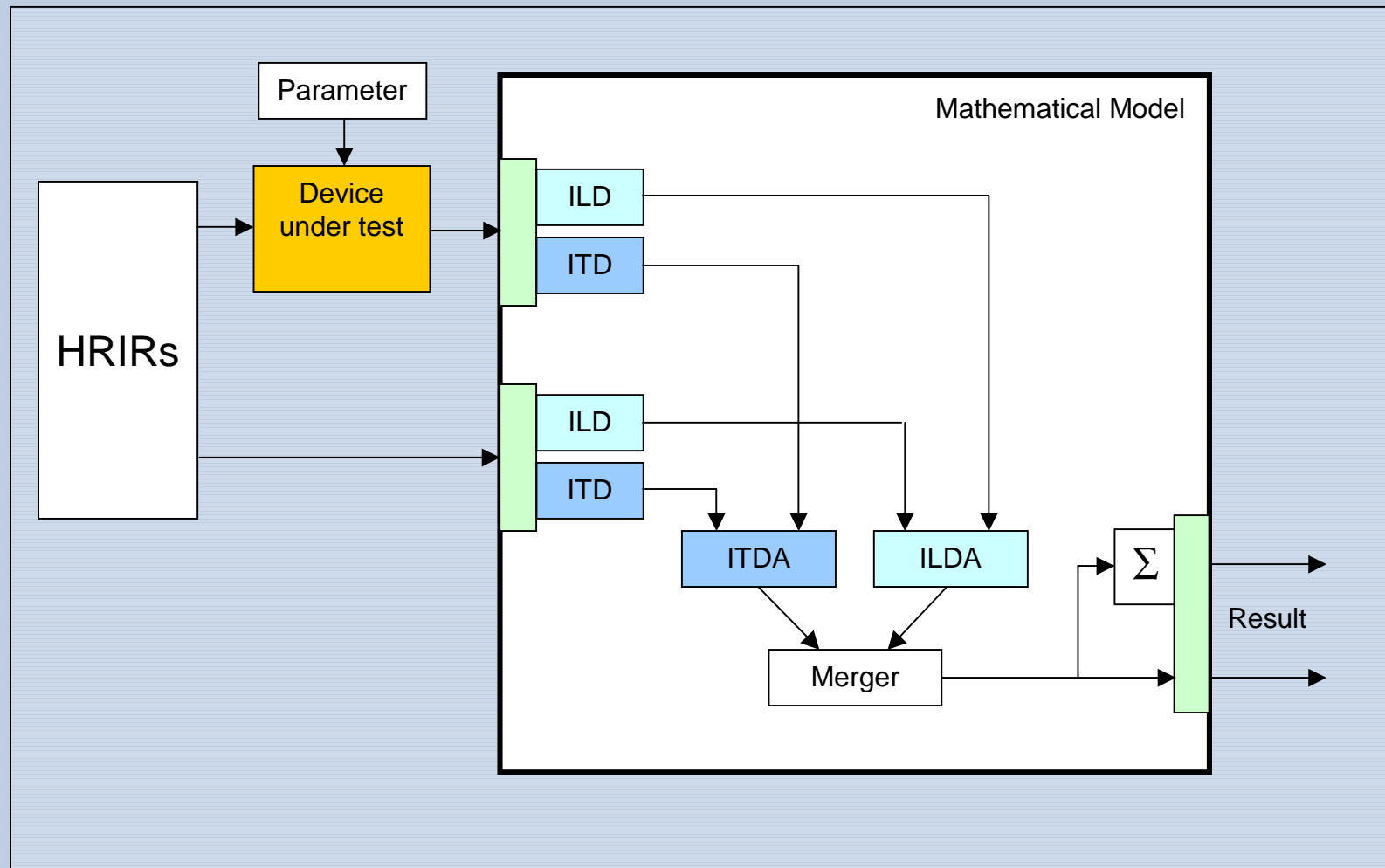
- classifying Binaural Reproduction Systems
- prediction of localisation performance

## Main assumption:

- the reference HRIRs result in optimal localisation
- 2D systems only



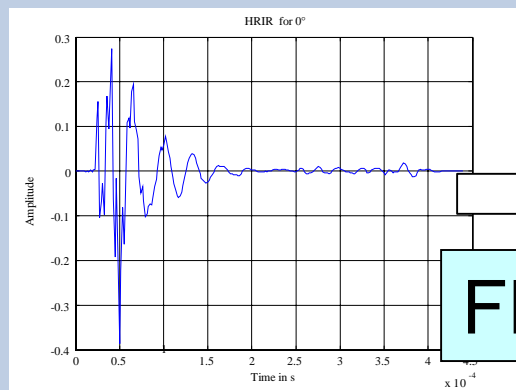
# Mathematical Model



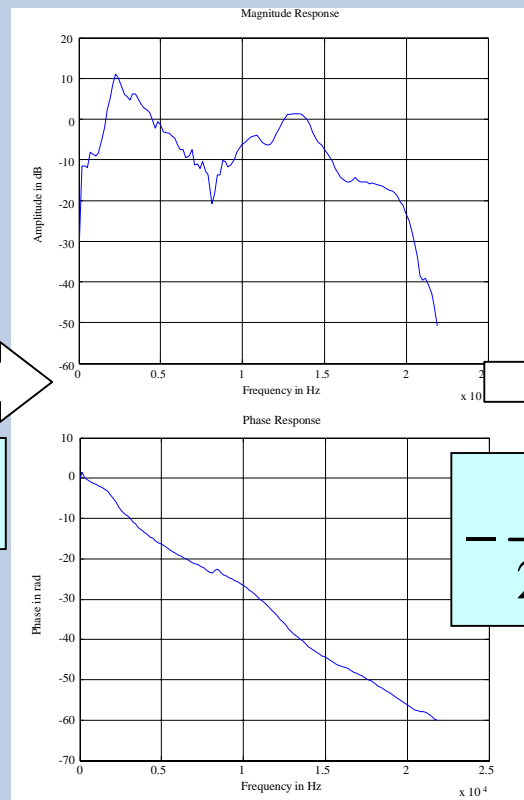


# Interaural Time Difference (ITD)

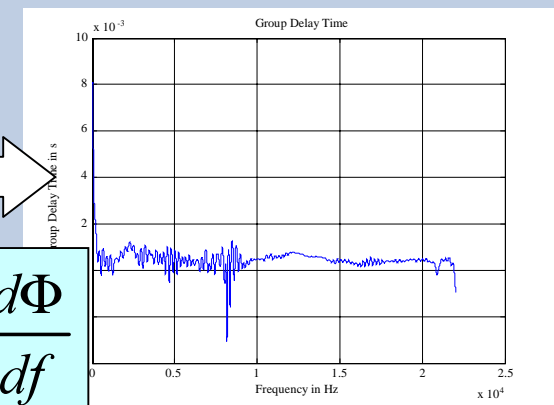
HRIR,  $\phi=0^\circ$



FFT



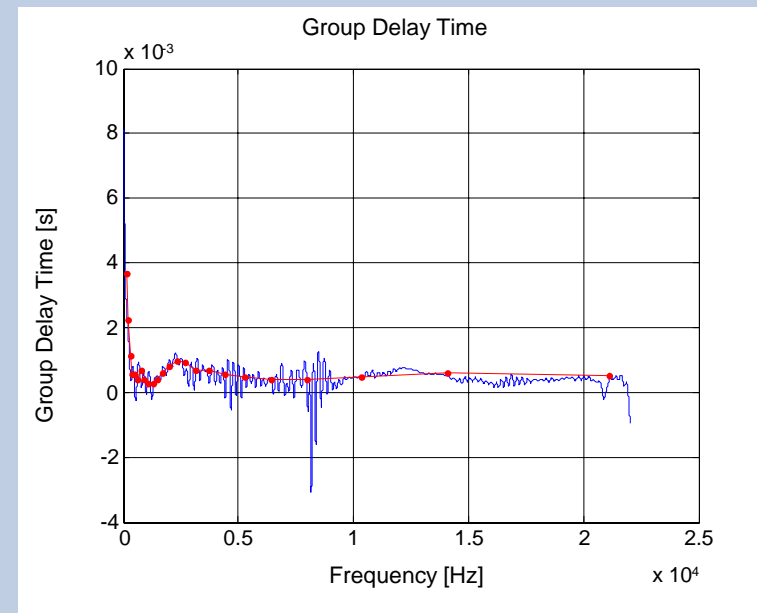
$$\frac{1}{2\pi} \cdot \frac{d\Phi}{df}$$



# Interaural Time Difference (ITD)

## Calculation of the group delay time:

- impulse response (HRIR)
- zero phase filter over critical bands
- energy center of gravity per band
- group delay time per band

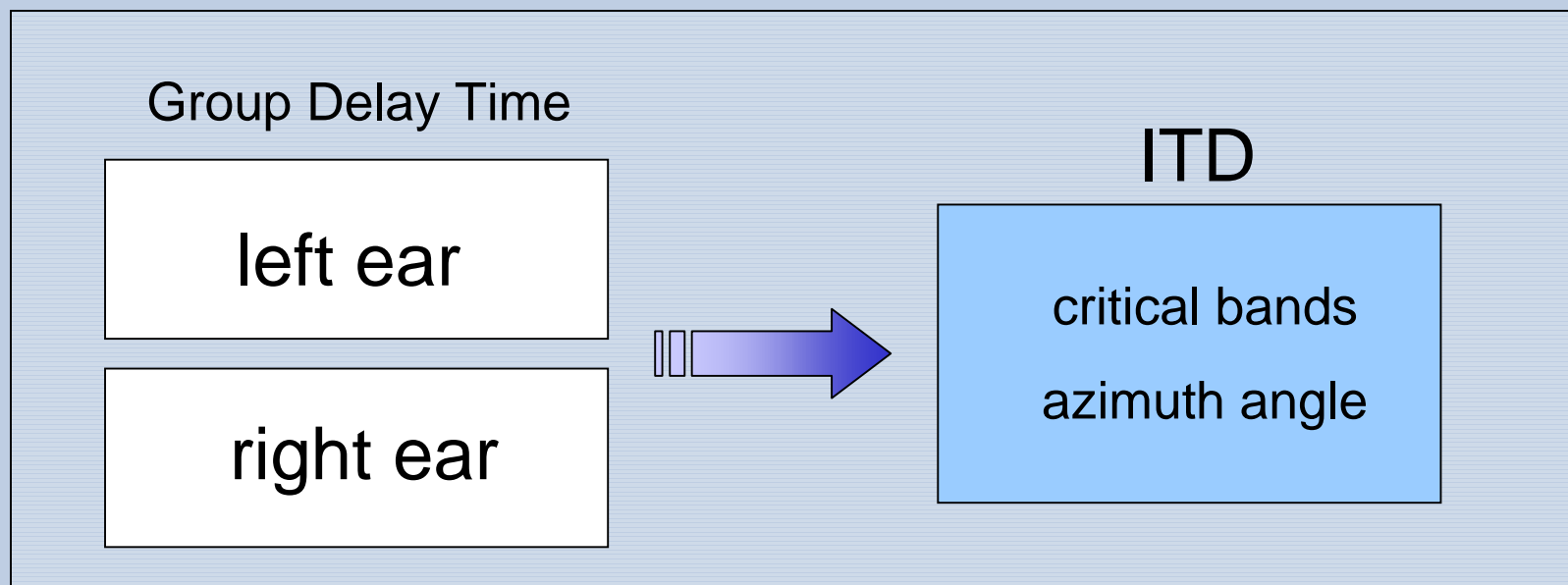


# Interaural Time Difference (ITD)

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ITD over critical bands:

difference of the group delay time between ipsi- and contralateral eardrum

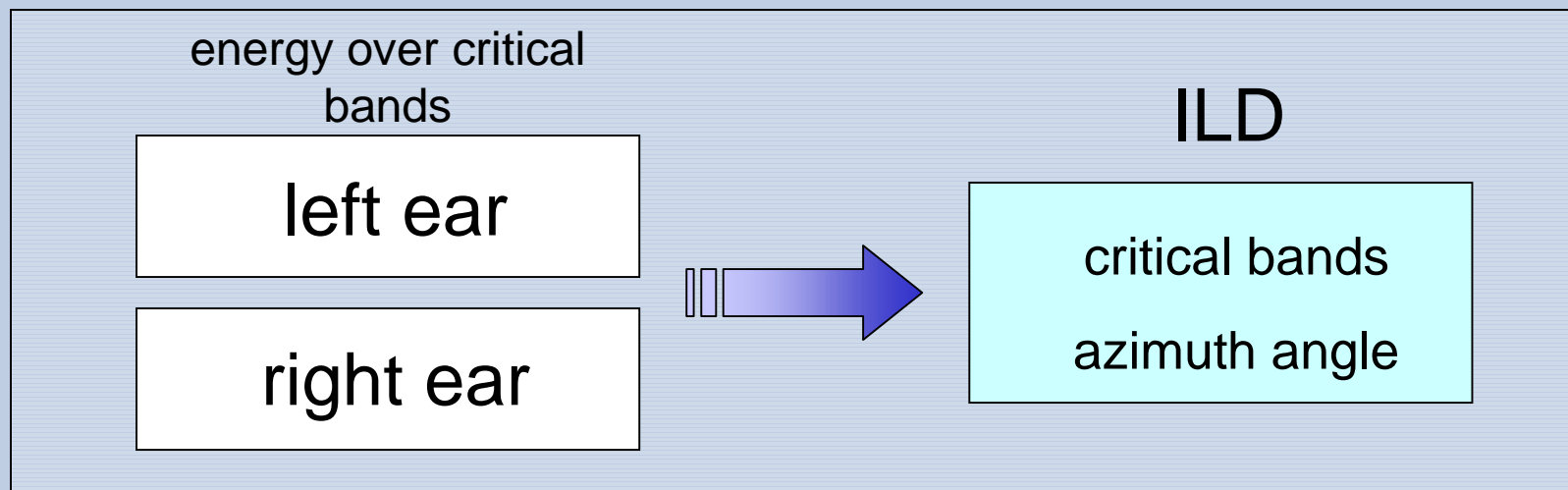


# Interaural Level Difference (ILD)

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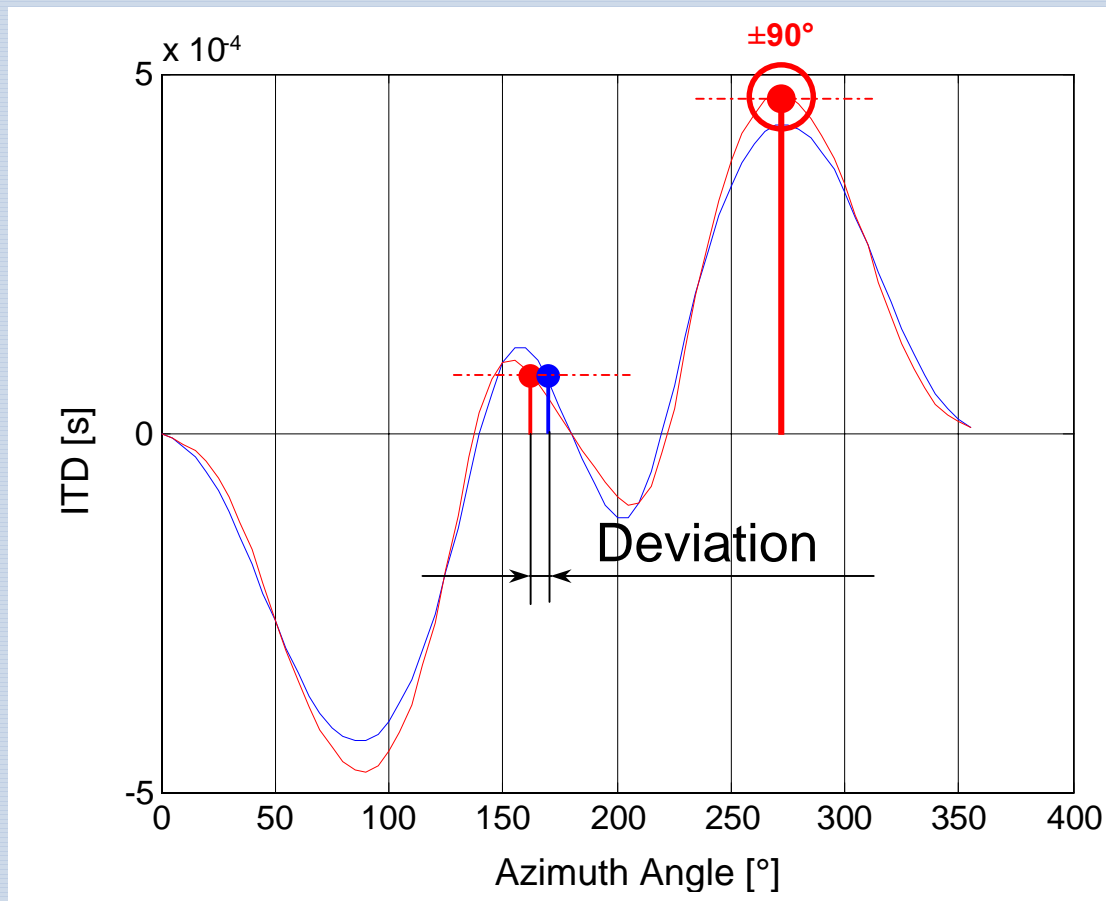
Calculation of the ILD:

- amplitude response (HRTF)
- energy-difference over critical bands between ipsi- and contralateral eardrums



# Interaural Difference Angle (ITDA/ILDA)

## Search Algorithm:

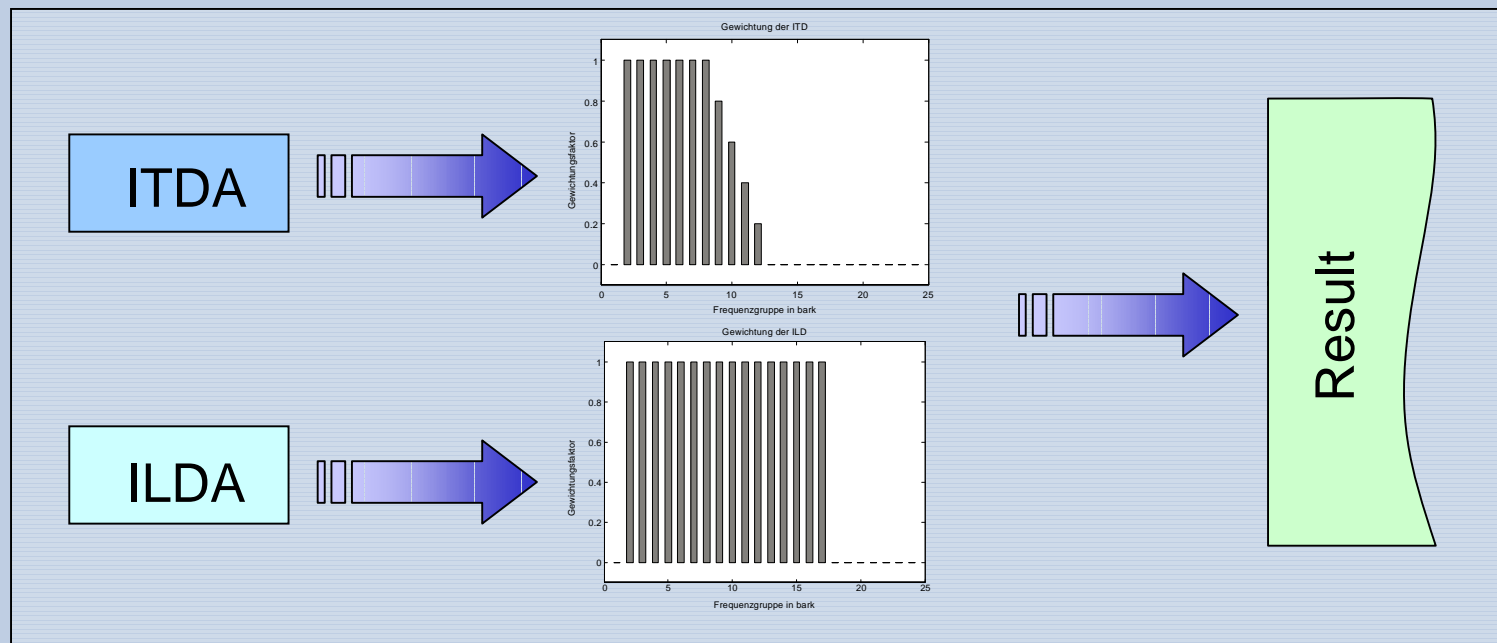


ITD for one critical band  
calculated from measured  
HRIR

- distorted ITD
- reference ITD

# Merging of ITDA and ILDA

- ITDA: fade out above 800 Hz
- ILDA: fully weighted



# Results (1)

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- **localisation function** (averaged over critical bands)

$$L(\Theta) = \frac{1}{2} \cdot \left( \frac{1}{\sum w_{ITD}(z)} \cdot \sum_{z=1}^{24} w_{ITD}(z) \cdot \Theta_{ITD}(z, \Theta) \right) + \frac{1}{2} \cdot \left( \frac{1}{\sum w_{ILD}(z)} \cdot \sum_{z=1}^{24} w_{ILD}(z) \cdot \Theta_{ILD}(z, \Theta) \right)$$

- **localisation blur** (standard deviation over critical bands)

$$Bl(\Theta) = \sqrt{\frac{1}{2} \cdot \sum_{i=ITD} \frac{1}{\sum w_i(z)} \cdot \sum_{z=1}^{24} w_i(z) \cdot [\Theta_i(z, \Theta) - L(\Theta)]^2}$$



## Results (2)

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- average localisation blur  
(averaged over the azimuth angle)

$$\bar{L} = \sqrt{\frac{1}{N} \sum_{i=1}^N [L(\Theta_i) - \Theta_i]^2}$$

- average localisation error  
averaged over azimuth angle referring to the MAA

$$\bar{Bl} = \frac{1}{N} \cdot \sum_{\Theta=0}^{360^\circ} \frac{Bl(\Theta)}{MAA(\Theta)}$$

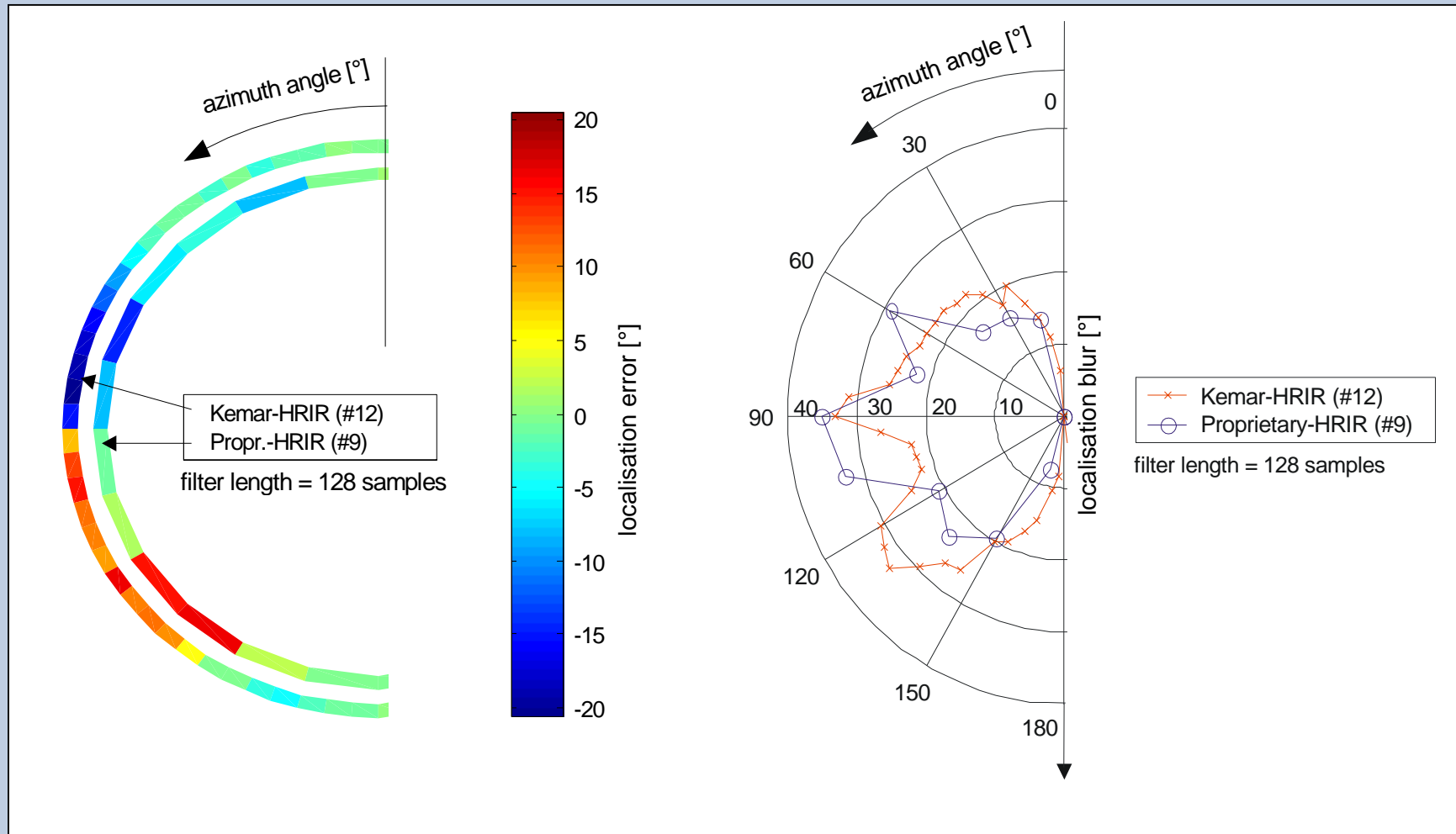
# Analysis

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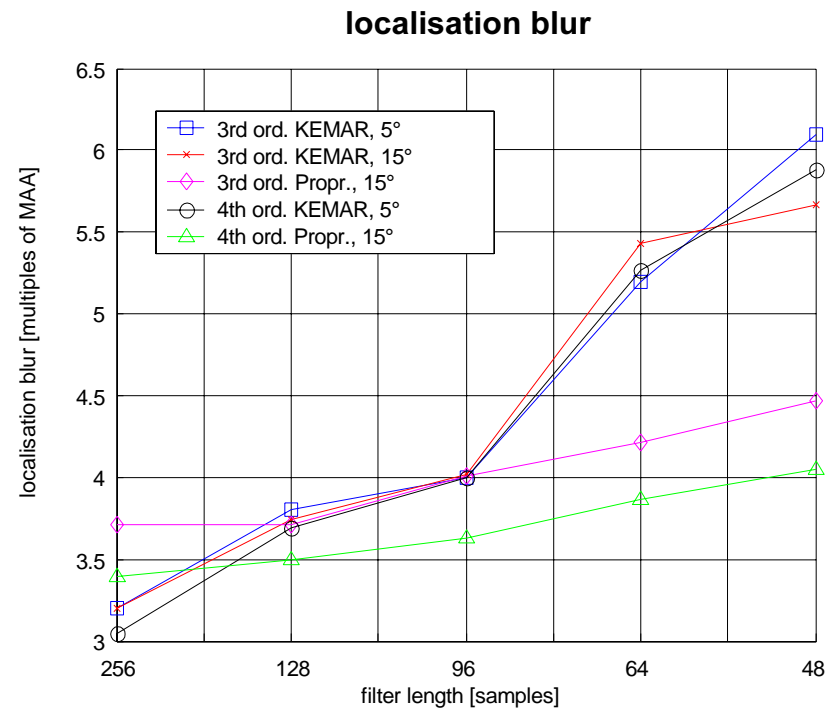
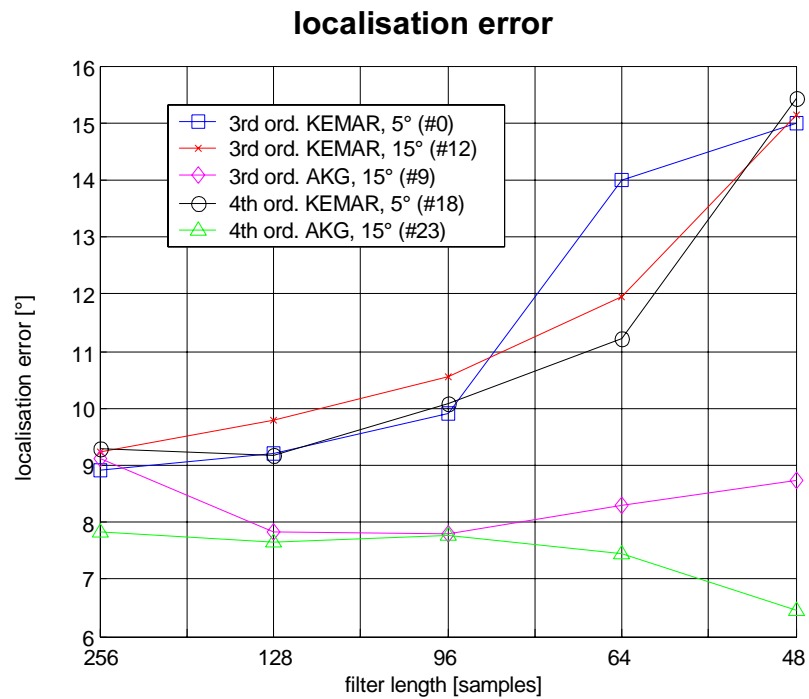
Variations of design parameters:

- reference HRIRs
- length of HRIR
- ambisonic order
- weighting of ambisonic channels
- number of virtual speaker

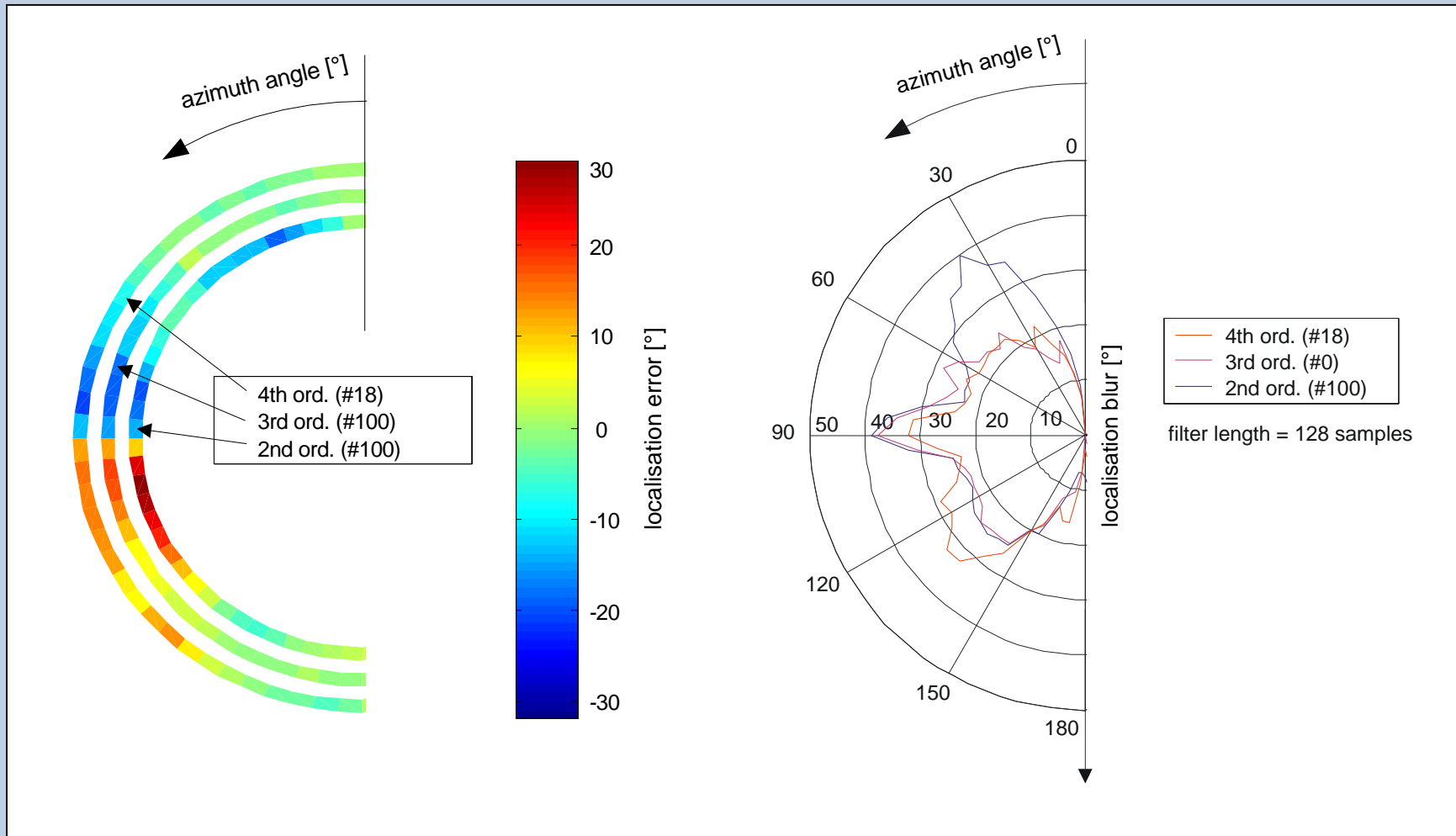
# HRIR Type (1)



# HRIR Type (2)

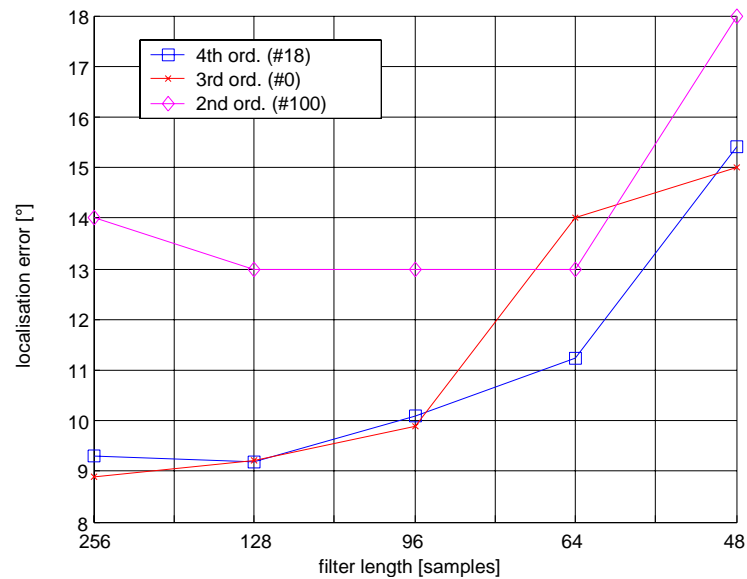


# Ambisonic Order (1)

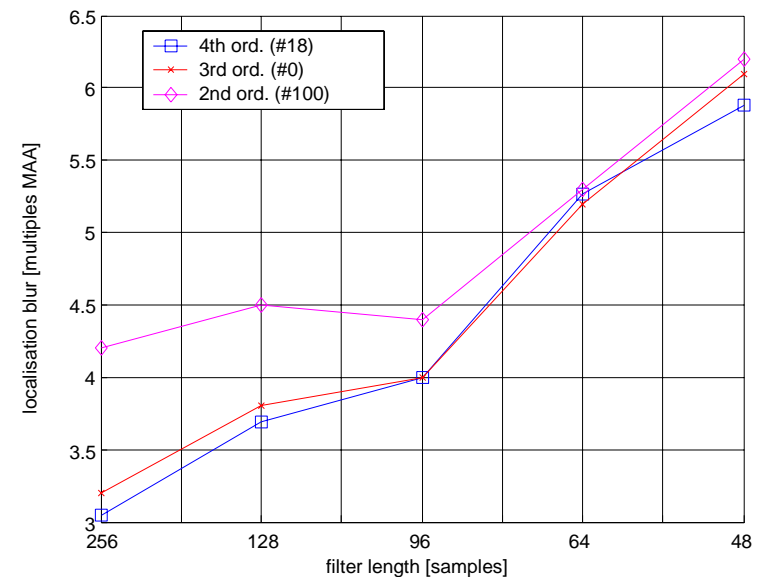


# Ambisonic Order (2)

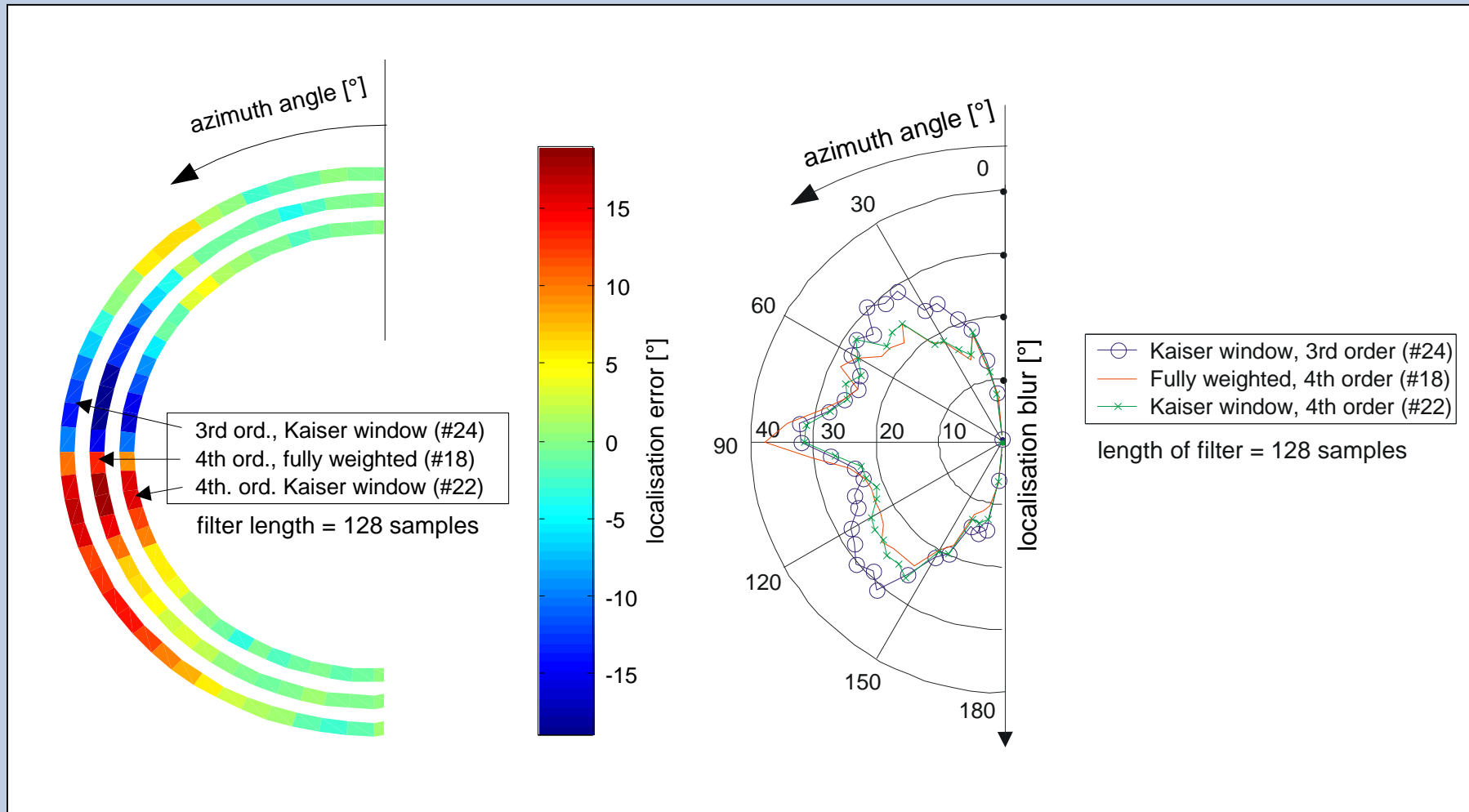
localisation error



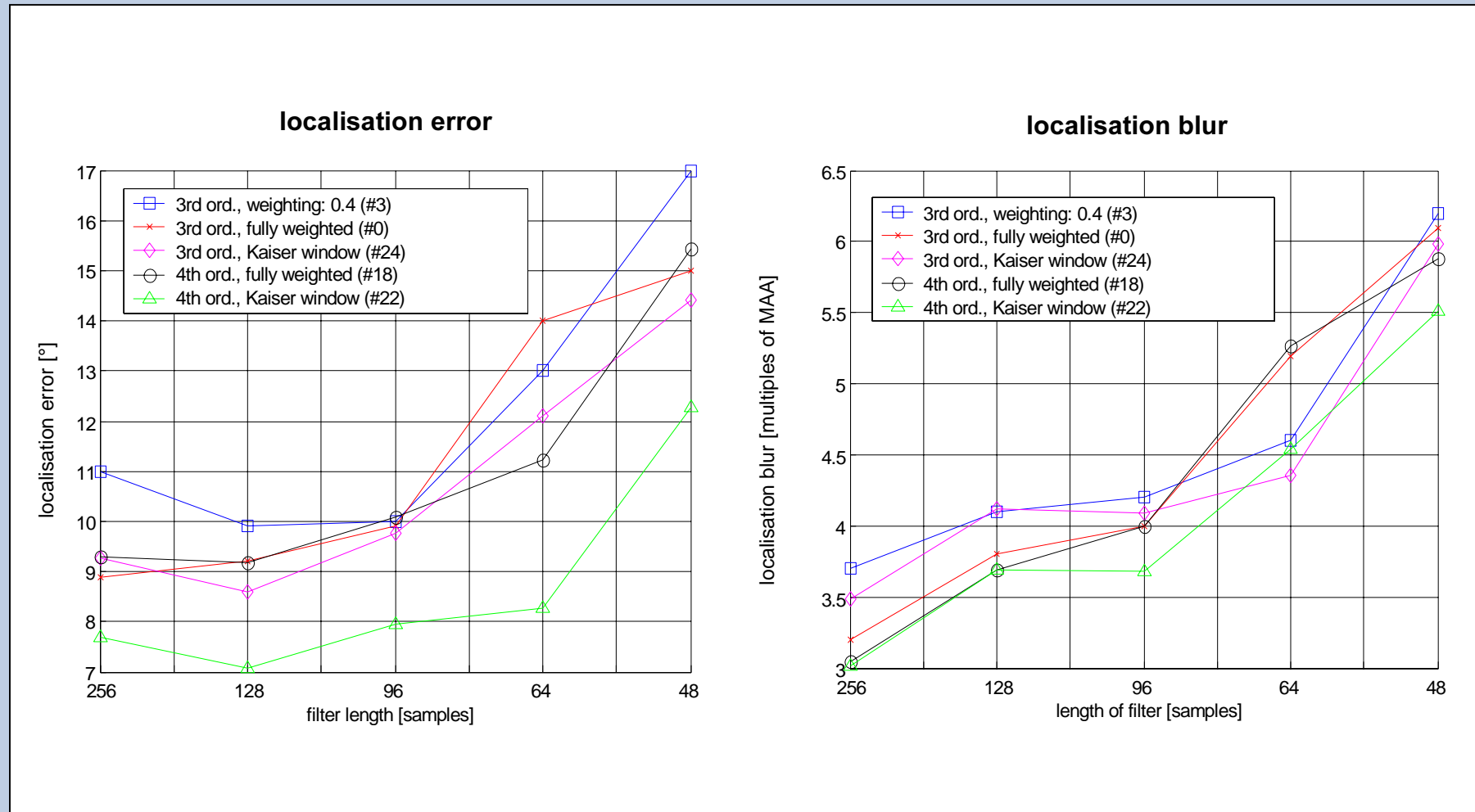
localisation blur



# Ambisonic Weighting (1)



# Ambisonic Weighting (2)





# Conclusion

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- prediction of localisation is possible
- results correspond with ambisonic theory
  - ambisonic not less than 3rd order for correct localisation
  - weighting of channels using Kaiser-window yields better localisation
  - filter length up to 128 samples
- model was evaluated using listening tests

# Outlook

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- incorporate IGD (*interaural group delay*) as a cue for high frequency localisation
- classification regarding coloration and externity
- extend the model for 3D applications
- warping tables to predict and minimise the localisation errors for further implementations



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**Thank you!**



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